Lecture 2: Non-phylogenetic transmission reconstruction

Epidemiological vs genomic outbreak reconstruction

Epidemiological outbreak data alone can be used for outbreak reconstruction (i.e. contact tracing), but genomic data offer a high-resolution source of information

What can genomic data offer?

- Extra detail
- Resolve transmission where epi data are hard to get and/or have gaps
- Genomic data becoming ever easier, cheaper and faster to obtain (e.g. real-time sequencing becoming possible)

Challenge: create a single framework/likelihood incorporating genomic + epidemiological data

Imagine we have 3 people infected in an outbreak...



We want to combine our genomic information and our epidemiological information, to best narrow down which possible path the infection took...



2 of the earliest approaches

Many of the earliest methods tackled the 2 data streams separately



Proc. R. Soc. B (2008) 275, 887–895 doi:10.1098/rspb.2007.1442 Published online 29 January 2008

Integrating genetic and epidemiological data to determine transmission pathways of foot-and-mouth disease virus

Eleanor M. Cottam^{1,2}, Gaël Thébaud^{2,†}, Jemma Wadsworth¹, John Gloster^{3,‡}, Leonard Mansley⁴, David J. Paton¹, Donald P. King¹ and Daniel T. Haydon^{2,*}



Cottam et al

- 3-step maximum likelihood approach
- Rank the likelihood of the set of plausible trees

Applied to 20 farms from 2001 UK Foot-and-mouth disease outbreak, to obtain a most likely transmission tree

Many of the earliest methods tackled the 2 data streams separately - Cottam et al process

Begin with a set of **all** possible transmission trees given the set of sampled cases

- 1. Select only trees that are consistent with **known infection pairs**
- 2. Select only remaining trees that are consistent with the genomic data
- 3. Calculate the **likelihood** of each remaining tree based on the **epi information** – describing both the chance each host (farm) was infected on a given day and able to infect others on a given day.

Many of the earliest methods tackled the 2 data streams separately - Cottam et al process

Begin with a set of **all** possible transmission trees given the set of sampled cases

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Also potentially demanding

Depending on the size of the data and how many trees you were able to exclude

Many of the earliest methods tackled the 2 data streams separately - Cottam et al process



Finally, either (a) pick 1 optimal tree, or (b) pick a set of optimal trees (and look for similarities between them)

> This is done by ranking the remaining trees by their likelihood

SeqTrack - a graph based approach

This method also tackles the genomic and then the epidemiological information

Heredity (2011) 106, 383–390 © 2011 Macmillan Publishers Limited All rights reserved 0018-067X/11 www.nature.com/hdy

ORIGINAL ARTICLE

/w.nature.com/ndy

Reconstructing disease outbreaks from genetic data: a graph approach

T Jombart, RM Eggo, PJ Dodd and F Balloux Department of Infectious Disease Epidemiology, MRC Centre for Outbreak Analysis and Modelling, Imperial College Faculty of Medicine, London, UK

- **Graph theory** approach to find 'genetically parsimonious' transmission trees
- Algorithm *SeqTrack* finds the optimum branching in a directed graph



a

b

c d

e



Genomic distance matrix								
	a	b	c	d	e	f		
a	0	1	3	2	5	9		
b		0	2	4	7	5		
c			0	1	4	12		
d				0	1	3		
e					0	8		
f						0		

(i) Create a connected, directed graph with weights w_{ij} equal to the genetic distance



c: t=2 f: t=7

Genomic distance matrix								
	a	b	c	d	e	f		
a	0	1	3	2	5	9		
b		0	2	4	7	5		
c			0	1	4	12		
d				0	1	3		
e					0	8		
f						0		

(i) Create a connected, directed graph with weights w_{ii} equal to the genetic distance

We do this every node, but lets restrict to (a) for simplicity...



Sample collection dates:

a: t=3	d: t=5
b: t=1	e: t=4
c: t=2	f: t=7

Genomic distance matrix								
	a	b	c	d	e	f		
a	0	1	3	2	5	9		
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(i) Create a connected, directed graph with weights w_{ij} equal to the genetic distance (ii) Remove edge ij if $t_j < t_i$ (iii) Find the spanning directed tree optimizing (i.e. minimizing) $\sum w_{ij}$



c: t=2 f: t=7

'This problem has been solved by Edmonds (1967) and Chu and Liu (1965), ... The algorithm proceeds by identifying optimum ancestors for each node at the exception of the root (the oldest isolate), and then recursively removes possible cycles. However, in our case, cycles are impossible as ancestries cannot go back in time, which greatly simplifies computations.'

	a	b	c	d	e	f
a	0	1	3	2	5	9
b		0	2	4	7	5
c			0	1	4	12
d				0	1	3
e					0	8
f						0



Sample collection dates:

c: t=2 f: t=7

Some limitations:

- All cases come from single index case e.g. a single sampled ancestor
- All cases are known and sampled
- Sampling times not used in weighting

SeqTrack also:

- Assumes that individuals became infectious in the order they are sampled
- Has no uncertainty in the output transmission tree or probabilistic parameters

But

- Fast, simple, explore all the possibilities

2 short primers for lecture 2

A quick primer 1: generation time and sampling time



Generation time = the time interval between the infection of an individual and their seeding of new secondary cases.

Sampling time = the time interval between infection and collection of an isolate.

A popular computational method for exploring complex and/or high-dimensional spaces – e.g. transmission trees

The main idea: $p(\theta|y) \propto p(y|\theta)p(\theta)$ Posterior distribution– the prior probability of our model parameters θ given the data y For us, we may have e.g. Θ = transmission tree and parameters controlling it y = sequences and epi data

When this quantity (the posterior) is hard to maximise directly, we instead form a Markov chain with equilibrium distribution equal to the posterior distribution, and take many samples from this chain.



Average length of books

1.0 0.8 0.6 Density 0.4 0.2 0.0 500 1000 1500 2000 0 Number of pages, Θ

Average length of books

Essentially, we approximate the posterior distribution by random sampling from a probabilistic space (of all possible books or all possible transmission trees).

Data-augmented MCMC is a method for dealing with missing data within an MCMC algorithm. As well as sampling from the parameter space at each step of the Markov chain, we also sample values for the missing data.

In transmission inference, missing data might be the time of infection of the cases (since typically we only know sampling times) or the number of unsampled cases, for example.

In actuality, the 'random' samples we collect in MCMC are not independent – they form a chain with *equilibrium* distribution equal to the target distribution.

The set of **X** samples at the start of the MCMC run are often discarded – it takes some time to reach an area of the state space with good posterior support. We call this initial set **X** the **burn-in**



Transmission reconstruction with outbreaker(2)

outbreaker and outbreaker2

We're going to look at these 2 methods in detail – and will be using them in the next exercise

These also create a unified likelihood for genetic + epidemiological data, but within a Bayesian framework, that allows more estimation and greater flexibility.

outbreaker vs outbreaker2

outbreaker2 is a more customisable version of outbreaker

We're mainly going to focus on the core outbreaker model...

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Data:

N sampled cases, each with genetic sequence s_i and time of sampling t_i

Quantities:

 $d(s_i, s_j)$ = number of mutations (distance) between sequences i and j $l(s_i, s_j)$ = number of nucleotide positions which can be compared i and jw = distribution of the generation time f = distribution of the sampling time

> 1:1999-08-01
GCACCCATTCCCGCCTGGAGAT
> 2:2007-11-01
GCACCCATTCCCGCCTAGAGAT



Thibaut Jombart*, Anne Cori, Xavier Didelot, Simon Cauchemez, Christophe Fraser*, Neil Ferguson

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Goal: find the most likely transmission tree



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Parameters:

 μ = mutation rate, per site per generation of infection π = proportion of unsampled cases are estimated as well as the transmission tree

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Posterior distribution:

$$P(A, \theta \mid D) = \frac{P(D, A \mid \theta) P(\theta)}{P(D)} \propto p\left(\left\{s_i, t_i, \alpha_i, \kappa_i, T_i^{\inf}\right\}_{i=1, \dots, N} \mid \mu, \pi\right) \times p(\mu, \pi).$$

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likelihood data augmented given prior the on param.s

param.s

Parameters:

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Posterior distribution:

$$P(A, \theta \mid D) = \frac{P(D, A \mid \theta) P(\theta)}{P(D)} \propto p\left(\left\{s_i, t_i, \alpha_i, \kappa_i, T_i^{\inf}\right\}_{i=1, \dots, N} \mid \mu, \pi\right) \times p(\mu, \pi).$$

All cases are assumed to be conditionally independent, given the identity of their most recent sampled ancestor, so the likelihood decomposes to:

$$p\left(\left\{s_{i}, t_{i}, \alpha_{i}, \kappa_{i}, T_{i}^{\inf}\right\}_{i=1,\dots,N} \mid \mu, \pi\right) = \prod_{i=2}^{N} p\left(s_{i}, t_{i}, \alpha_{i}, \kappa_{i}, T_{i}^{\inf} \mid s_{\alpha_{i}}, t_{\alpha_{i}}, T_{\alpha_{i}}^{\inf}, \mu, \pi\right) \times p(t_{1} \mid T_{1}^{\inf})p(s_{1})p\left(T_{1}^{\inf}\right)p(\alpha_{1})p(\kappa_{1})$$

Parameters:

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These terms relate only to initial case

One point to note: since cases may share a common unsampled ancestry, this is technically a composite (approximate) likelihood

$$p\left(\left\{s_{i}, t_{i}, \alpha_{i}, \kappa_{i}, T_{i}^{\inf}\right\}_{i=1,\dots,N} \mid \mu, \pi\right) = \prod_{i=2}^{N} p\left(s_{i}, t_{i}, \alpha_{i}, \kappa_{i}, T_{i}^{\inf} \mid s_{\alpha_{i}}, t_{\alpha_{i}}, T_{\alpha_{i}}^{\inf}, \mu, \pi\right) \times p(t_{1} \mid T_{1}^{\inf})p(s_{1})p\left(T_{1}^{\inf}\right)p(\alpha_{1})p(\kappa_{1})$$

The pseudo-likelihood is further decomposed into genetic and epidemiological components. For each case i = 1, ..., N:



Genetic part

The outbreaker genetic model assumes no within-host genetic diversity, and so mutations are direct features of transmission events. All transmission events are assumed independent, and the genetic pseudo-likelihood is very fast to compute.

Genetic pseudo-likelihood of case i = the probability of observing genetic



= the probability of observing genetic distance $d(s_i, s_{\alpha_i})$ between sequence s_i and the ancestral sequence s_{α_i} with iand α_i separated by κ_i generations.

As a method designed for shorter timescale outbreaks, reverse mutations are considered negligible.

Genetic pseudolikelihood =

$$\mu^{\mathrm{d}(s_i,s_{\alpha_i})} (1-\mu)^{\kappa_i \times \mathrm{l}(s_i,s_{\alpha_i}) - \mathrm{d}(s_i,s_{\alpha_i})}$$

Describes the probability of... Time of infection given

Time of sampling given time of infection

knowledge of infector

 $p(t_i | T_i^{\text{inf}}) p(T_i^{\text{inf}} | \alpha_i, T_{\alpha_i}^{\text{inf}}, \kappa_i) p(\kappa_i | \pi)$

Number of missing cases given rate of missing cases

$$F\left(t_{i} - T_{i}^{\inf}\right) \times w^{\kappa_{i}}\left(T_{i}^{\inf} - T_{\alpha_{i}}^{\inf}\right) \times \text{NB}(1 | \kappa_{i} - 1, \pi)$$

probability of obtaining one 'success' (sampling a case) after $\kappa_i - 1$ 'failures' (unobserved cases), with probability of success π .

Remember:

w = distribution of the generation time

= distribution of the sampling time



That forms the core of the outbreaker model.

The likelihood expressions introduced in the previous slides are combined with priors for the mutation rate μ and proportion of unsampled cases π .

μ is given a uniform prior on [0,1] – corresponding to an assumption of scarce prior information on this
 π is given a beta distributed prior with parameters controlled by the user of outbreaker. This is a flexible prior which can reflect different levels of prior knowledge for different datasets.

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The authors also introduce a method for detecting **imported cases** – i.e. cases that are not descended from another case in the outbreak.

In an initial step of the model, genetic outliers are detected, relative to the other samples in the dataset. A 'global influence' GI_i is calculated for each sampled case, defined as

$$GI_i = \mathbb{E}\left(\sum_{j=1, j \neq i}^n GPL_j\right) - \mathbb{E}\left(\sum_{i=1}^n GPL_i\right)$$

where *GPL* is the genetic pseudo-likelihood. This is calculated over the first few samples of the MCMC, say 50.

A large value of the GI_i implies unlikely numbers of mutations i.e. a 'distant' sequence. Cases with a global influence more than 5 times the average across all cases are considered outliers.

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$$GI_{i} = \mathbb{E}\left(\sum_{j=1, j\neq i}^{n} GPL_{j}\right) - \mathbb{E}\left(\sum_{i=1}^{n} GPL_{i}\right) \quad \begin{cases} \text{Des} \\ GPL \\ \end{bmatrix}$$

Describes what proportion *i*'s GPL is of the total GPL

where *GPL* is the genetic pseudo-likelihood. This is calculated over the first few samples of the MCMC, say 50.

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An application from

Data from 2003 Singaporean Severe Acute Respiratory Syndrome (SARS) outbreak. 13 genomes with <15 mutations between all pairs.

Generation time = Γ (mean 8.4, SD 3.8) Same sampling time

Bayesian Reconstruction of Disease Outbreaks by Combining Epidemiologic and Genomic Data

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An application from

Data from 2003 Singaporean Severe Acute Respiratory Syndrome (SARS) outbreak. 13 genomes with <15 mutations between all pairs.

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How to get here from the posterior expression?

- 1. Run MCMC to sample many trees (and many μ , π , ... values)
- 2. Pick a consensus tree that best represents the set

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Campbell *et al. BMC Bioinformatics* 2018, **19**(Suppl 11):363 https://doi.org/10.1186/s12859-018-2330-z

BMC Bioinformatics

outbreaker2: extensions

SOFTWARE

Open Access



outbreaker2: a modular platform for outbreak reconstruction

Finlay Campbell, Xavier Didelot, Rich Fitzjohn, Neil Ferguson, Anne Cori and Thibaut Jombart *



• Combines an R package with C++ code for efficiency, through Rcpp

- Can customise all these facets of the package
- For example, they implemented the TransPhylo methodology, which we will work with tomorrow, in outbreaker2.